



Development of a Regression Model of Dependence of Territorial Development of the Republic of Tatarstan on Implementation of Infrastructure Projects

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ABSTRACT: The article is devoted to development of a model of regression dependence of territorial development of Republic of Tatarstan on implementation of infrastructure projects. The relevance of the studied issues is due to a number of factors. The main ones are: satisfaction of infrastructure needs of the population in the form of a range of services and, as a result, improving the quality of life of the population. In addition, infrastructure projects in modern realities are tools for the implementation of strategic plans. As elements of federal and regional development programs, they are included in the group of priority national projects approved by the President of the Russian Federation. According to experts, infrastructure projects can become drivers of the socio-economic development of territories of various levels, bringing them to a new level of existence. Thus, the built-up regression model of dependence is aimed at identifying the role of infrastructure projects in the territorial development of the Republic of Tatarstan. On the way to achieving the goal, the stages of the development of the methodology are shown with a detailed description of the methods used, the rationale for their use in relation to the specifics of the Tatarstan region is presented, the difficulties encountered and the chosen ways to overcome them are described, and the conclusions are presented. The result of the study was a regression model with socio-economic indicators of the dependence of the gross territorial product of the municipal regions of the republic on the financing of infrastructure projects in them. Verification of the model showed its compliance with all Gauss-Markov conditions, which proves its applicability for predicting the process in the region.

Keywords: Infrastructure projects, territorial development, regression dependence, project management, strategic planning, econometric modeling, regional economy.

I. INTRODUCTION

Modern realities call for considering infrastructure projects not only as objects of providing services to the population and satisfying needs, but as integrated drivers of territorial development that can bring the region to a new level of socio-economic development [10]. In connection with this understanding of infrastructure projects, it is advisable, using econometric methods, to find out their role for the purposes of territorial development. In addition, the relevance of the topic is due to the fact that infrastructure projects are the basic tools for the implementation of strategic planning goals, which are currently being actively developed in Russia and the Republic of Tatarstan in particular. The basic concepts and paradigms of social and economic geography used in the work are: industry paradigm (infrastructure geography), regional paradigm, system-structural approach [6]. An analysis of the problems associated with the nature and practice of project risk management was carried out by Srinivas [8]. Issues of the methodology and conceptual framework of social design during the implementation of regional development projects have been thoroughly investigated by famous scientists - Smyth and Vanclay [9].

The study was conducted on the example of Republic of Tatarstan- one of the leading regions in the socio-economic development of Russian Federation. The object was infrastructure projects as a factor in the territorial development of the region's economy. The main goal is, on the basis of theoretical and methodological approaches to the content of infrastructure projects, to find out their roles in ensuring the ongoing socio-economic development of the territory (for example, Republic of Tatarstan).

II. METHODS

Considering the infrastructure project primarily as a driver of territorial development, it is advisable to use indicators reflecting the development of the territory (region, municipal district) to assess its implementation. In this regard, the following factors were chosen as the explanatory factors for building an econometric model: "number of infrastructure projects" and their "financing by municipal districts of the Republic of Tatarstan", and the gross territorial product (GTP) of the municipalities of the Republic of Tatarstan was adopted as the explained indicator.

Thus, the main method was the econometric model of the regression dependence of the selected indicators. The selection consisted of 27 municipal districts of the Republic of Tatarstan (including 2 urban districts: Kazan and Naberezhnye Chelny, which act as independent subjects). The choice of this number of analyzed units is due to the presence in them of implemented infrastructure projects by the reporting period of 2017. The statistics are taken from the website of the Ministry of Economy of the Republic of Tatarstan, the source is the Plan for the creation of infrastructure facilities in the Republic of Tatarstan [1].

The econometric model of paired regression was tested according to Gauss-Markov conditions, during which conclusions were made about the presence and strength of the correlation relationship between factors, the statistical significance of factors was evaluated, the overall quality level of the model was checked, and the conditions of the absence of heteroscedasticity and multicollinearity were verified. As a result, conclusions were made about the possibilities of practical use of the model for the purposes of forecasting the development of processes, taking into account the strategic goals.

III. RESULTS AND DISCUSSION

In our work, we used the multiple regression model (in this case, it is given by two explanatory variables x_1 and x_2), which has the form [5]:

$$y = \hat{f}(x_1, x_2, \dots, x_k)$$

where y is the explained variable (GTP); x_1, x_2 - explaining variables (number of infrastructure projects,

financing of infrastructure projects in municipal districts of the Republic of Tatarstan).

Baseline data are presented in Table 1 [1, 4].

The selection consists of 27 units. Accordingly, $n = 45$, $m = 2$.

First, we construct the matrix R [5].

$$R = \begin{pmatrix} 1 & & & \\ Ryx_1 & 1 & & \\ Ryx_2 & Rx_1Rx_2 & 1 & \end{pmatrix} |$$

Table 1.

| Municipalities | | GTP | Number of projects | Project financing |
|----------------|-------------------|------------|--------------------|-------------------|
| S.No. | Name | y | x_1 | x_2 |
| 1 | Kazan | 604300 | 48 | 3288999,687 |
| 2 | NaberezhnyeChelny | 163300 | 24 | 1394336.3 |
| 3 | Agryzsky | 6553.7 | 1 | 1814 |
| 4 | Aznakaevsky | 45330 | 1 | 598 |
| 5 | Aktanyshsky | 9000 | 3 | 3065,181 |
| 6 | Almetyevsky | 253,000 | 6 | 692,336.69 |
| 7 | Bugulminsky | 47461 | 1 | 1018.2 |
| 8 | Buinsky | 9792.9 | 2 | 3002.5 |
| 9 | Verkhneuslonsky | 4895.8 | 3 | 35 |
| 10 | Vysokogorsky | 14037 | 1 | 2270.6 |
| 11 | Drozhzhanovsky | 5420 | 2 | 2302.5 |
| 12 | Yelabuzhsky | 35,500 | 19 | 1666729,79 |
| 13 | Zainsky | 29300 | 2 | 48320 |
| 14 | Zelenodolsky | 33200 | 11 | 24647,8 |
| 15 | Kukmorsky | 8898.2 | 1 | 1815 |
| 16 | Laishevsky | 19608,4 | 15 | 124546,4466 |
| 17 | Leninogorsk | 58800 | 1 | 28866.9 |
| 18 | Mamadyshsky | 7370 | 1 | eight |
| 19 | Mendeleevsky | 12,400 | 4 | 45632,657 |
| 20 | Menzelinsky | 5081 | 1 | 6000 |
| 21 | Nizhnekamsky | 172100 | 19 | 482844.92 |
| 22 | Pestrechinsky | 6183.3 | 3 | 2452.24 |
| 23 | Rybno-Slobodsky | 4746 | 8 | 2719,308 |
| 24 | Sabinsky | 10210.75 | 4 | 1819.1 |
| 25 | Sarmanovsky | 22851.5 | 1 | 70 |
| 26 | Tukaevsky | 31700 | 3 | 1714.04 |
| 27 | Chistopolsky | 14329.8 | 2 | 4347.5 |
| Σ | | 1635369.35 | 187 | 7832312.36 |
| Average | | 60569,2352 | 6.9259 | 290085,6429 |

(1) Calculate multicollinearity and correlation coefficients using the formulas [5]:

$$R_{x_1x_2} = \frac{\sum(x_{i1} - \bar{x}_1)(x_{i2} - \bar{x}_2)}{\sqrt{\sum(x_{i1} - \bar{x}_1)^2 * \sum(x_{i2} - \bar{x}_2)^2}} = 0,9249$$

$$R_{x_1y} = \frac{\sum(x_{i1} - \bar{x}_1)(y_i - \bar{y})}{\sqrt{\sum(x_{i1} - \bar{x}_1)^2 * \sum(y_i - \bar{y})^2}} = 0,8394$$

$$R_{x_2y} = \frac{\sum(x_{i2} - \bar{x}_2)(y_i - \bar{y})}{\sqrt{\sum(x_{i2} - \bar{x}_2)^2 * \sum(y_i - \bar{y})^2}} = 0,8723$$

It is worth noting the significant link between the explanatory variables and the factor y ($r_{xy} \geq 0.7$), however, due to the fact that the multicollinearity of the variables x_1 and x_2 was revealed ($R_{x_1x_2} = 0,9249$), then one of the factors must be excluded. The connection x_2 with y is slightly higher than with x_1 , therefore the further model will be lined up in a steam regression format with variables x_2 and y [5].

Paired regression is a model with two variables - y and x , i.e. view model [5]:

$$(y = \hat{f}(x))$$

where y is the explained variable (GTP); x - explanatory variable (financing of infrastructure projects).

Next, you need to find b_0 and b_1 from the formulas shown below [5].

$$b_0 = y - b_1 \bar{x} = 17773,8647$$

$$b_1 = \frac{\bar{xy} - \bar{x} * \bar{y}}{x^2 - (\bar{x})^2} = 0,1475$$

The next step is the verification of the resulting model to Gauss-Markov conditions.

For a start, it is worth noting that the positive sign of the coefficient b_1 shows the unidirectionality of x_2 and y changes, that is, with an increase in funding for infrastructure projects, the GTP in the municipality also increases, and vice versa [5].

(1) Already calculated the sample correlation coefficient ($r_{x_2y} = 0.8723$) indicates a significant relationship of variables [5]. Thus, we conclude that on the basis of the correlation coefficient, x_2 must be present in the model.

(2) Let us turn to the calculation of the statistical significance of the analyzed model of the pair regression.

To do this, it is necessary to calculate the indicator t_{calc} , having previously calculated such indicators

as: Sbj, S^2_{bj}, S_0^2 . The formulas and calculation results are presented below [5].

$$t_{calc} = \left| \frac{b_j}{s_{bj}} \right| = 8,9215$$

$$Sbj = \sqrt{S^2_{bj}} = 0,165$$

$$S^2_{bj} = \frac{1}{\sum(x_i - \bar{x})^2} * S_0^2 = 0,0003$$

$$S_0^2 = \frac{\sum e_i^2}{n-m-1} = 3829537863,6944$$

t_{calc} allows to make a conclusion about the statistical significance of the explanatory variable. Since $t_{calc} \geq 3$, therefore the factor x_2 is strongly significant [2].

3) The model is checked for the level of overall quality by calculating [5]:

$$F_{calc} = \frac{R^2}{1-R^2} * \frac{n-m-1}{m} = 79,5766$$

$$R^2 = 1 - \frac{\sum e_i^2}{\sum(y_i - \bar{y})^2} = 0,7609$$

From the obtained R^2 value, we can conclude that the factor x_2 explains the behavior of y by about 76%.

From Table Fischer define F_{cr} (for $\alpha = 0,05, V1 = m = 1, V2 = n-m-1 = 25$)

$$F_{kr} = 4,245$$

$F_{calc} > F_{kr}$, therefore the model has a good level of quality [2].

4) It is also necessary to make a check for the absence of autocorrelation of residuals. For this, there are the DW method and the series method, we will use both.

(a) DW method. We calculate this indicator by the formula [5]:

$$DW = \frac{\sum(e_i - e_{i-1})^2}{\sum e_i^2} = 1,9741$$

According to the Durbin-Watson table ($n = 27, m = 1$), we find critical points, they are schematically shown in Fig. 1.

$$Dl = 1,316$$

$$Du = 1,469$$

$$4 - Dl = 2,684$$

$$4 - Du = 2,531$$

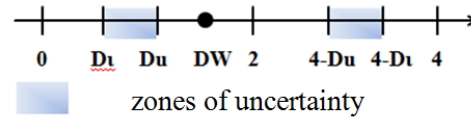


Fig. 1. Critical points and areas of uncertainty for the DW model.

As can be seen from the graph, DW does not fall into the zone of uncertainty, but enters the interval ($d_l \leq DW \leq 4 - d_u$), there is therefore no autocorrelation [2; 5].

b. Row method.

For this method, it is necessary to write out the characters in a row with the indicator ϵ for the entire sample population. We get the following sequence:

+ - + - + + - - - - + + - + - - - + - - - + + -

The number of sequences: $k = 14$.

The number of positive signs: $n1 = 10$.

The number of negative characters: $n2 = 17$.

According to the table of critical values for the series method, we find the lower ($k1 = 8$) and upper ($k2 = 19$) boundaries.

$k = 14$ falls into the interval (8; 19); therefore, there is no autocorrelation of residuals [2, 5].

Both methods confirmed the absence of autocorrelation of residuals.

5) We will check for heteroscedasticity. To do this, fill in the following Table 2 [5].

Table 1.

| x_2 | N_{x_2} | $ e_i $ | Ne_i | di | di^2 |
|-------------|-----------|-------------|--------|------|--------|
| 3288999,687 | 27 | 101310,9488 | 25 | 2 | 4 |
| 1394336,3 | 25 | 60175,6596 | 23 | 2 | 4 |
| 1814 | 7 | 11487,7734 | 10 | -3 | 9 |
| 598 | 4 | 27467,9190 | 20 | -16 | 256 |
| 3065,181 | 15 | 9226,0560 | 8 | 7 | 49 |
| 692336,69 | 24 | 133088,0095 | 26 | -2 | 4 |
| 1018,2 | 5 | 29536,9283 | 21 | -16 | 256 |
| 3002,5 | 14 | 8423,9088 | 6 | 8 | 64 |
| 35 | 2 | 12883,2234 | 15 | -13 | 169 |
| 2270,6 | 10 | 4071,8341 | 1 | 9 | 81 |
| 2302,5 | 11 | 12693,5402 | 14 | -3 | 9 |
| 1666729,79 | 26 | 228160,9657 | 27 | -1 | 1 |
| 48320 | 21 | 4397,6510 | 3 | 18 | 324 |
| 24647,8 | 18 | 11789,9320 | 11 | 7 | 49 |
| 1815 | 8 | 9143,4209 | 7 | 1 | 1 |
| 124546,4466 | 22 | 16539,3833 | 19 | 3 | 9 |
| 28866,9 | 19 | 36767,5022 | 22 | -3 | 9 |
| 8 | 1 | 10405,0402 | 9 | -8 | 64 |
| 45632,657 | 20 | 12105,8942 | 13 | 7 | 49 |
| 6000 | 17 | 13578,0201 | 17 | 0 | 0 |
| 482844,92 | 23 | 83093,6339 | 24 | -1 | 1 |
| 2452,24 | 12 | 11952,3308 | 12 | 0 | 0 |
| 2719,308 | 13 | 13429,0305 | 16 | -3 | 9 |
| 1819,1 | 9 | 7831,4758 | 5 | 4 | 16 |
| 70 | 3 | 5067,3131 | 4 | -1 | 1 |
| 1714,04 | 6 | 13673,2734 | 18 | -12 | 144 |
| 4347,5 | 16 | 4085,4322 | 2 | 14 | 196 |

For further calculations, we need to calculate the sum of squares in di . In our example, it is equal to: $\sum di^2 = 1778$ [5].

Next, we calculate the indicators r_{xe} (Test Spearman) and t_{calc} according to the following formulas [5]:

$$r_{x|e|} = 1 - 6 \frac{\sum di^2}{n(n^2-1)} = 0,4573$$

$$t_{\text{calc}} = \left| \frac{r_{x|e|} \sqrt{n-2}}{\sqrt{1-r_{x|e|}^2}} \right| = 2,5708$$

$R_{x|e|} \in [0.3; 0.7]$, we can conclude that the relationship exists. According to a rough estimate $t_{\text{calc}} \in [2; 3]$, which means that the factor x_2 is significant. Calculate t_{cr} on Student's table ($\alpha = 0.05, v = n - m - 1 = 25$). $t_{\text{cr}} = 2.06$ [5].

Conclusion: $t_{\text{calc}} > t_{\text{cr}}$ - heteroscedasticity is present [2].

This indicates the presence of sufficient data scatter. Attempting to eliminate heteroscedasticity by eliminating units from the model that make up less than 0.5% of the mean value in x_2 did not produce results. Therefore, in order to level this problem and eliminate heteroscedasticity, we use the Box-Jenkins method [5].

According to him, it is considered that the magnitude of the deviations depends on the magnitude of the explanatory variables.

$$\sigma_i^2 = \sigma^2 * x_i^2$$

Consequently, the model is converted from the form: for $y = b_0 + b_1 * x_i$ to a model of the following form [5]:

$$\frac{y_i}{x_i} = b_0 * \frac{1}{x_i} + b_1$$

To estimate it, it is necessary to recalculate the initial data ($x_i; y_i$) to ($x_i^*; y_i^*$) as follows [5]:

$$x_i^* = \frac{1}{x_i}; \quad y_i^* = \frac{y_i}{x_i}$$

For the new selection, we calculate the model, which is given by the following equation: $y = b_0 * x_i^* + b_1$, where b_0^* is the coefficient of the explaining variable b_1^* is the free term of the equation.

The formulas and calculations for b_0^* and b_1^* are presented below [5].

$$b_1^* = \frac{\bar{x}y^* - \bar{x}^* \bar{y}^*}{x^{*2} - (\bar{x}^*)^2} = \frac{113,7981}{0,0155} = 7337,2897$$

$$b_0^* = \bar{y} - b_1^* \bar{x} = 58,1935 - 7337,2897 * 0,0065 = 10,4783$$

Now that we have found the values of b_0^* and b_1^* , we will calculate this model, first of all we are interested in checking for heteroscedasticity. Similar calculations, but with the substitution of new values of the parameters, given the result of d^2 is equal to 2470.5 [2].

Calculate the indicator $r_{x|e|}$:

$$r_{x|e|} = 1 - 6 \frac{\sum d_i^2}{n(n^2-1)} = 0,2459$$

Check the result of student statistics.

$$t_{\text{calc}} = \left| \frac{r_{x|e|} \sqrt{n-2}}{\sqrt{1-r_{x|e|}^2}} \right| = 1,2683$$

According to a rough estimate $t_{\text{calc}} \in [1; 2]$, which means that the factor x_2 is weak. Calculate t_{cr} on Student's table ($\alpha = 0.05, v = n - m - 1 = 25$). $t_{\text{cr}} = 2,060$.

Conclusion: $t_{\text{cr}} > t_{\text{calc}}$ - heteroscedasticity is absent [2].

For the initial dependence, the equation takes the following form: $y = b_0 + b_1 * x_i$. According to the theory of econometrics, it is guaranteed that there is no heteroscedasticity. Thus, the applied Box-Jenkins method allowed us to eliminate heteroscedasticity in the model [5].

We will also make a prediction on the model obtained using the example of the Nizhnekamsk municipal district. For the planned period until 2020, this municipality plans to finance infrastructure projects in the amount of 3 million rubles [3]. Thus, calculating the value of y by the model equation, we obtain a value equal to 22022.3474 (y is also measured in million rubles), thus, it can be seen that funding for this amount will allow an increase in GTP by about 13% (calculated relative to $y = 172100$) (GTP in the prices of the reporting period of

2017 excluding inflation and the forecast of GTP dynamics for the planning period up to 2020) [7].

Check the result of student statistics

IV. SUMMARY

Thus, the developed model of the regression dependence of the gross territorial product on the costs of infrastructure projects in the municipal regions of the Republic of Tatarstan has proved its worth by checking for compliance with the Gauss-Markov conditions. The study proved the statistical significance of the explanatory indicator, significant correlation of indicators. The direct dependence of the selected coefficients was revealed: financing of infrastructure and gross territorial product in the municipalities of the republic. For a specific example, a predictive calculation is made. The role of infrastructure projects for the progressive socio-economic development of the region is proved.

V. CONCLUSIONS

In conclusion, we note that with the recalculation of the regression model, she went through all the stages of checking the Gauss-Markov conditions, during which it was determined that there was no autocorrelation of residuals in the model (proved by DW and row methods) and heteroscedasticity (this item was made possible by recalculating Box-Jenkins models).

Estimates proved the unidirectionality of the changes explaining and explaining the variable (with an increase in the financing of infrastructure projects in the municipality the gross territorial product grows), a high level of correlation of variables ($r_{x_2y} = 0.8723$) and statistical significance of the parameter ($t_{\text{calc}} = 8.9215$; $t_{\text{calc}} \geq 3$).

Conclusions about a good quality level of the model were made ($F_{\text{calc}} > F_{\text{cr}}$). It was also determined that the financing of infrastructure projects by about 76% determines the value of the gross territorial product in the municipal districts of the Republic of Tatarstan.

Thus, this model can be used in practical activities, including for the calculation of projected indicators of GTP changes for the municipal districts of the Republic of Tatarstan, depending on the allocated funding for infrastructure projects.

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