

### Evaluation of Stress - Strain Relation on Rotational Motion of a Rotating Disc

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ABSTRACT: The effect of change due to angular speed on stable state creep behaviour of a rotating functional graded aluminium silicon carbide particle disc is examined by using Sherby's law. The stress and strain is obtained by taking pressure, volume and temperature constant with varying angular speed. It is investigated that the increase in the angular speed results in the increase of stress as well as strain in the rotating disc at two different angular speed of the disc.

Keywords: Composite, functionally graded material, rotational motion, creep, Sherby's law.

#### I. INTRODUCTION

Rotating discs have various engineering assumptions such as steam and gas turbine rotors, high speed gear engine, turbo generators, interior start engines, turbojet motors, responding and centrifugal compressors just to specify several. These applications perform components in conditions of effective services, life and power transportation are based on material speed of rotating and also working conditions other assumptions such as in aerospace engineering in which the various factors such as weight and durability at elevated temperature environment are so vital [27]. They have used FGM as special material. FGM are the combinations ceramic and metal. The ceramic materials provide elevated temperature resistance because of its low thermal conductivity. On different side the ductile metal prevent fracture caused by stress because of elevated temperature gradient in short time period. Steady -state strain rates in a rotating disk can be proscribed by choosing most favourable particle content and size of reinforcement. The thickness and density, stresses and strains in an elastic perfectly plastic isotropic revolving disk of consistent thickness and density by von Mises yield criteria [10]. Wahl et. al., [1] calculated secondary creep deformation in revolving disk by von Mises and Tresca yield criteria theoretically as well as experimentally. He has concluded that the creep deformations calculated using von Mises criteria are too low in comparison to experimental results, which may be due to the anisotropy of the material used. Ma (1959) the shear stress theory is used to study the solid disc in a metallic gas at constant gas elevated temperature. The analysis is extended for gas turbine and jet engine disc to determine to the stress distributions over middle part of disk having variable thickness are moderately unique in relation to those apparent in a disc of consistent thickness. The exponential creep law is used to describe Secondary creep. Pandey et al. (1992) [5] analyzed the affect of volume fraction and size of reinforcement on the balanced state deformation behaviour of Al-SiCp composites with temperature ranging 623 to 723k. The observation resulted that the stress exponents are more than 15 and empty activation is 294 KJ/mol. It was observed that the stress strain rate behaviour of composite arranged with stress dependent sub structure in variant model.

Jahed and Dubey (1997) [6] analysed primary, secondary deformation in axis symmetric problem in case of rotating disks and pressure vessels have been done. The technique uses the basic solution for a rotating uniform isotropic disc and generates the solution for non-uniform inhomogeneous one. Primary creep and secondary creep behaviour have been studied using anticipated method. Gupta et al. (2000) [7] examined that creep stresses rates and strain rates in a disk of variable thickness and density using Seth's transition theory. The result was obtained that the disk with density and thickness proportion diminishes is on more secure side as compare to flat disc having variable density. Singh et al., [10] considered the effect of presence of residual stress on the rotating disc by using Norton's power law while comparing it with strain rate in disc without residual stress. You et al., (2007) [13] implemented a simple method based on axis symmetric plane strain and steady state creep to determine stress and strain on functional graded material (FGM) of cylindrical vessels which were subjected to internal pressure. Singh et al., [16] performed creep analysis on an isotropic 6061 Al-20vol% SiCw disc at the speed of 15000 rpm at temperature 561k by using Nortan's power law. Chen et al., [17] experimented the coefficient of thermal expansion and aggregated plastic strain of pure Al-Matrix made of 50% silicon carbide particles within temperature 298 to 573k these disc contain SiC particle in matrix of pure aluminium. Rattan et al., [18] explored the stable state deformation reaction of an isotropic functional graded material rotating disk of aluminium silicon carbide particle composites exposed to molecule inclination utilizing Sherby's law and inferred that the drag conduct in the disk can be constrained by the appropriate circulation of molecule substance as the strain rates are least when molecule substance is dispersed illustratively along the radial distance of disk. Thakur et al., (2013-2016) [21] observed the problem of rotating disk with thermal effect and heat generation due to variable thickness by using Seth's transition theory. Gupta et al., (2016) [23] discussed the variant of Poisson ratios and thermal creep stresses also strain rates in an isotropic disc.

Thakur *et al.*, (2017) [27] examined the influence of thermal gradient on the stable state creep of the disk for three different cases. First case is the set at the uniform temperature of 625k while in the second case the

temperature is 52k at inner radii and outer radii as 658k and 588k in the third case the disc operates at 110 k.

Singh et al., (2018) [28] compared selective properties of composite material they examine Al-SiC have been best material, having high dissolving element, over the top thermal and electric conductivity and erosion resistance. Al-SiC have over the top tensile, right exhaustion, break habitations, high dissolving element, extreme flexibility, electric conductivity and great erosion resistance. Steel have malleable, over the top capacity to weight proportion due to this that has unnecessary vitality in saving through unit mass, metal gadgets may be small and light weight, never again like different building substances, steel can be impacts manufactured and generation colossally, bendy, sensibly estimated however steel is an alloy of iron. Silicon carbide (SiC) has high hardness, high thermal stability, low thermal increment, electric conductivity. SiC has many advantage utilized for high voltage, high temperature utility. The main aim of this paper is to evaluate the values of stress and strain in the rotating disk at various angular velocities.

#### **II. ESTIMATION OF CREEP PARAMETERS**

The balanced state creep reaction of the aluminum silicon carbide particle composite of changeable composition is depicted as far as of Sherby threshold stress based model given by

$$\frac{1}{\varepsilon} = [M(\overline{\sigma} - \sigma_0)]^8$$
  
where, 
$$M = \frac{1}{E} \left[\frac{AD_L \lambda^3}{\left|\overline{b_r}\right|^5}\right]^{1/8}$$
(1)

where,  $\sigma$  is effective stress, "M" is material creep constant, D<sub>L</sub> is the lattice diffusivity,  $\lambda$  is the sub grain size, A is the constant,  $|\overrightarrow{b_r}|$  is the magnitude of Burger's

vector, E is the young's modulus,  $\sigma_0$  is the threshold stress.

After obtaining, values of creep parameters "M" and  $\sigma_0$ These have been fit in the regression equation in the function of particle size, volume % and temperature. It has been determined that P = 1.7  $\mu m$ , V = 10% and T = 623 k.

In M=(-34.91+0.2112 In P+ 4.89 In I-0.59 In V) (2)  

$$\sigma_0 = (-0.03507P + 0.01057T + 1.00536V - 2.11916)$$
 (3)

#### **III. MATHEMATICAL FORMULATION**

-Consider a disk of aluminium silicon carbide (Al-SiC) of constant width having inner radii a, outer radii b revolving at angular speed and the applications are

Secondary condition of stress is supposed.

Elastic deformations being relatively little for disk and may be ignored as compared to the creep deformation.
The thickness is small as compared to its diameter

therefore they assumed that axial stress is zero on the faces of disk.

-For biaxial state of stress, the globalized constitutive equations for deformation in an isotropic composite take the accompanying form when reference frame use along the principal directions r and z.

$$\dot{\varepsilon}_{r} = \frac{\varepsilon}{2\bar{\sigma}} \Big[ 2\sigma_{r} - \sigma_{\theta} \Big]$$
$$\dot{\varepsilon}_{\theta} = \frac{\dot{\varepsilon}}{2\bar{\sigma}} \Big[ 2\sigma_{\theta} - \sigma_{r} \Big]$$

$$\dot{\varepsilon}_{z} = \frac{\dot{\overline{\varepsilon}}}{2\overline{\sigma}} \Big[ -(\sigma_{r} + \sigma_{\theta}) \Big]$$
(4)

where,  $\mathcal{E}_r, \mathcal{E}_{\theta}, \dot{\mathcal{E}}_z$  are strain rates and  $\sigma_r, \sigma_{\theta}, \sigma_z$  stresses correspondingly in direction r,  $\theta$ , z as indicate by subscripts.

Assuming that effective stress is based on mises criterion (1913, for biaxial state of stress, effective stress,  $\overline{\sigma}$  is given as,

$$\overline{\sigma} = \frac{1}{\sqrt{2}} \left[ \sigma_r^2 + \sigma_\theta^2 + (\sigma_r - \sigma_\theta)^2 \right]^{1/2}$$
(5)

Using Eqns. (1) and (5) in consti. Eqn. (4), one gets,

$$\varepsilon_{\rm r} = \frac{{\rm d}\mu_{\rm r}}{{\rm d}r} = \frac{[{\rm M}(\overline{\sigma} - \sigma_{\rm 0})]^8(2{\rm x} - 1)}{2[{\rm x}^2 - {\rm x} + 1]^{1/2}} \tag{6}$$

$$\varepsilon_{\theta} = \frac{\mu_{\rm r}}{\rm r} = \frac{[{\rm M}(\overline{\sigma} - \sigma_{\rm 0})]^8 (2 - {\rm x})}{2[{\rm x}^2 - {\rm x} + 1]^{1/2}}$$
(7)

$$\dot{\varepsilon}_{z} = \frac{-[M(\bar{\sigma} - \sigma_{0})]^{8}(x+1)}{2[(x)^{2} - x + 1]^{1/2}}$$
(8)

where,  $x = \sigma_r / \sigma_{\theta}$  is ratio of radial and tangential stress over any radii r. eqns.(6) and (7) can be calculated to attain  $\sigma_{\theta}$  which is given by,

$$\sigma_{\theta} = \frac{(\dot{u}_{a})^{1/8}}{M} \psi_{1} + \psi_{2}$$
(9)

where 
$$\dot{u}_{a}^{1/8} = \frac{\int_{a}^{b} M \sigma_{\theta} dr - \int_{a}^{b} M \psi_{2} dr}{\int_{a}^{b} \psi_{1} dr}$$

$$=\frac{\psi}{\left[\frac{1}{1-2}\right]^{1/2}}$$
(11)

$$\psi_2 = \frac{\sigma_0}{\left[x^2 - x + 1\right]^{1/2}}$$
(12)

$$\psi = \left[\frac{2\left[x^2 - x + 1\right]^{1/2}}{r(2 - x)} \exp \int_{a}^{r} \frac{\phi}{r} dr\right]^{\overline{a}}$$
(13)

and

$$\phi = \frac{(2x-1)}{(2-x)}$$
(14)

The stability of forces in radial direction are

$$\frac{\mathrm{d}}{\mathrm{d}\mathbf{r}}\left[\mathbf{r}\,\boldsymbol{\sigma}_{\mathrm{r}}\right] - \boldsymbol{\sigma}_{\theta} + \rho\omega^{2}\mathbf{r}^{2} = 0 \tag{15}$$

Int. Eqn. (15) from r = a to r = b and also putting the boundary condition  $\sigma_r = 0$  at r = a and boundary

condition  $\sigma_r = 0$  at r = b one gets,

$$\int_{a}^{b} \sigma_{\theta} d\mathbf{r} = \rho \omega^{2} (b^{3} - a^{3}) / 3$$
(16)

In the first iteration,  $\sigma_{\theta} = \sigma_{\theta_{avg}}$ , where  $\sigma_{\theta_{avg}}$  is average tang. Stress over cross segment of disk. Therefore (10) in first iteration is

$$\dot{u}_{a}^{1/8} = \frac{\sigma_{\theta_{avg}} \int_{a}^{b} Mdr - \int_{a}^{b} M\psi_{2}dr}{\int_{a}^{b} \psi_{1}dr}$$
(17)

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The values of  $\sigma_r$  can be obtained

$$\sigma_{\rm r} = \frac{1}{\rm r} \int_{\rm a}^{\rm r} \sigma_{\theta} \, \mathrm{dr} - \frac{\rho \omega^2 ({\rm r}^3 - {\rm a}^3)}{3{\rm r}} \tag{18}$$

Finding the values of  $\sigma_{\theta}$  from Eqn. (9) radial stress  $\sigma_{r}$  is found by Eqn.(18) any point in composite disk also strain rate  $\dot{\varepsilon}_{r}$  and strain rate  $\dot{\varepsilon}_{\theta}$  is calculate from the Eqns. (6), (7) resp.

#### **IV. NUMERICAL RESULTS**

The strain and stress distribution of rotating aluminium silicon carbide particle (Al-SiC<sub>p</sub>) disc rotating motion at 13000 rpm and 15000 rpm are evaluated from the above mathematical modelling.

# Table 1: Represents numerical calculation of radial/tangential stress and strain at different rotational motion of a rotating disc.

Angular speed	Radii	Radial/tangential stress and strain
<i>w</i> =13000	r=40	$\sigma_r = 0.8072 * 10^{15}$
		$\sigma_{\theta}$ = 4.7398 * $10^{15}$
		$\mathcal{E}_r = -3.4783 \times 10^{98}$
		$\hat{e}_{\theta} = 9.0651 * 10^{98}$
<i>Ѡ</i> =15000	r=40	$\sigma_r = 0.3455 * 10^{16}$
		$\sigma_{\theta}$ = 1.8899 * $10^{16}$
		• $\mathcal{E}_r = -23.2715 * 10^{103}$
		$\mathcal{E}_{\theta} = 66.66 * 10^{103}$
<i>@</i> =13000	r=60	$\sigma_r = 1.7007 * 10^{15}$
		$\sigma_{\theta}$ = 4.7396 * $10^{15}$
		$\mathcal{E}_r = -1.0165 * 10^{98}$
		• $\mathcal{E}_{\theta} = 5.9248 * 10^{98}$
<i>₩</i> =15000	r =60	$\sigma_r = 0.8064 * 10^{16}$
		$\sigma_{\theta}$ = 1.8898 * $10^{16}$
		$\mathcal{E}_r = -0.7160 * 10^{103}$
		$\mathcal{E}_{\theta} = 7.9435 * 10^{103}$
<i>w</i> =13000	r=80	$\sigma_r = 1.8727 * 10^{15}$
		$\sigma_{\theta}$ = 4.7391* 10 <sup>15</sup>
		$\mathcal{E}_r = -0.7237 * 10^{98}$
		$\mathcal{E}_{\theta} = 5.5611 * 10^{98}$
		$\sigma_r = 0.9997 * 10^{16}$

		-
<i>@</i> =15000	r=80	$\sigma_{ heta}$ = 1.8889 * $10^{16}$
		• $\mathcal{E}_r = -1.1939 * 10^{103}$
		$\mathcal{E}_{\theta} = 3.1339 * 10^{103}$
<i>w</i> =13000	r=100	$\sigma_r = 1.6719 * 10^{15}$
		$\sigma_{\theta}$ = 4.7389 * $10^{15}$
		• $\mathcal{E}_r = -1.0654 * 10^{98}$
		• $\mathcal{E}_{\theta} = 5.9809 * 10^{98}$
<i>€</i> /2=15000	r=100	$\sigma_r = 1.0748 * 10^{16}$
		$\sigma_{ heta}$ = 1.8877 * $10^{16}$
		$\mathcal{E}_r = -0.2991 * 10^{103}$
		• $\mathcal{E}_{\theta} = 3.1177 * 10^{103}$
<i>w</i> =13000	r=120	$\sigma_r = 1.2210 * 10^{15}$
		$\sigma_{ heta}$ =4.7385 * $10^{15}$
		$\mathcal{E}_r = -2.0760  10^{98}$
		$\mathcal{E}_{\theta} = 7.470710^{98}$
<i>₩</i> =15000	r=120	$\sigma_r$ =1.0826 * $10^{16}$
		$\sigma_{ heta}$ =1.8876 * $10^{16}$
		$\mathcal{E}_r = -0.3180 * 10^{103}$
		$\mathcal{E}_{\theta} = 3.1171 * 10^{103}$
<i>Ѡ</i> =13000	r=140	$\sigma_r$ =0.5732 * $10^{15}$
		$\sigma_{\theta}$ =4.7384 * $10^{15}$
		$\mathcal{E}_r = -4.6098 * 10^{98}$
		• $\mathcal{E}_{\theta} = 11.4299 * 10^{98}$
<i>Ѡ</i> =15000	r=140	$\sigma_r$ = 1.0449 * 10 <sup>16</sup>
		$\sigma_{\theta}$ = 1.8872 * $10^{16}$
		$\mathcal{E}_r = -0.2234 \times 10^{103}$
		$\mathcal{E}_{\theta} = 3.0419 * 10^{103}$

## IV. DISCUSSION AND GRAPHICAL REPRESENTATION

Fig. 1 represents the radial stress plotted at the angular speed 13000 rpm. It is examined that the radial stress is elevated at middle of disk as compared inner radii and outer radii. In the given Fig. 2, the radial stress is concluded at the angular speed 15000 rpm, it is examined that at inner radii the radial stress is lower

and with increase in the radius of disk the radial stress again starts decreases. In Fig. 3, examined that the tangential stress is elevated at inner radii by increases the radial distance then tangential stress will decreases. The tangential stress is plotted at the angular speed 13000 rpm. It has



Fig. 1. Variation of radial stress along radial distance with Composite disk at the 13000 rpm







Fig. 3. Variation of tangential stress along radial distance with Composite disk at the 13000 rpm.

goes on raising but at the outer radii the radial stress



**Fig. 4.** Variation of tangential stress along radial distance with Composite disk at the 15000rpm.

In given Fig. 4, the tangential stress is plotted at the angular speed 15000 rpm. It is examined that the tangential stress is increases at inner radii and it starts decreases while increases the radius. In figure 5, the radial strain is concluded at the angular speed 13000 rpm. It is examined that the radial strain is elevated at the centre of the disk and lesser at the inner radius and outer radius. Also, outer radii are less radial strain than inner radii.



Fig. 5. Variation of radial strain along the radial distance with Composite disk at 13000 rpm.



Fig. 6. Variation of radial strain along the radial distance with Composite disk at 15000 rpm.





In given Fig. 6, the radial strain is plotted at the angular speed 15000rpm it is examined that radial strain is lesser at the inner radii and it starts increases while we increase the radius and maximum at outer radius. In Fig. 7, the tangential strain is concluded at the angular speed 13000 rpm. It is examined that the tangential strain is higher at inner radii and outer radii of disk. The outer radii are more than inner radius and it is less at the middle of the disc. In Fig. 8, the tangential strain is concluded at the angular speed 15000rpm. It is examined that tangential strain is higher at inner radii and it starts decreases with the increase of radius and at the outer radii tangential stress is less. In the given Fig. 9, the radial stress along the radius at angular speed 13000/15000rpm is higher at centre of the disk. The radial stress higher for the disk rotating at 15000rpm as compared to the disk rotating at 13000rpm.



Fig. 8. Variation of tangential strain along radial distance with Composite disk at 15000 rpm.









In the given Fig. 10, tangential stress is represented along radius at angular speed 13000/15000 rpm. It is found that tangential stress at 15000 rpm is higher than angular speed of 13000 rpm. In this given Fig. 11, the radial strain is represented along radius at the angular speed 13000 rpm/15000 rpm. It is examined that the radial strain at the 13000rpm is higher than 15000 rpm at the inner radii and at the outer radii. In Fig. 12, the tangential strain is represented along radius at angular speed 13000/15000 rpm. It is found that tangential strain at the 15000 rpm is higher than 13000 rpm at the inner radii.









#### V. CONCLUSIONS

It has been concluded that by increases in angular speed radial/tangential stress and strain is increased over entire radii in the isotropic disc operating at different angular speed. This analysis may be useful whenever one is interested in safe design of a rotating disk at high angular speeds

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